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SOLVING GEOMETRIC PROGRAMS USING GRG-RESULTS AND COMPARISONS

BY

M. RATNER, L.S. LASDON and A. JAIN

TECHNICAL REPORT SOL 76-1 MAY 1976

Systems Optimization Laboratory

Department of Operations Research

Stanford University



Stanford California 94305

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### Introduction

This paper describes the performance of a generalized reduced gradient (GRG) algorithm in solving geometric programs. The code used, described in [5], is a general purpose nonlinear programming code, and takes no advantage of the structure of geometric programs. First partial derivatives of the objective and all constraint functions are required, and these are computed by simple forward difference approximations. All problem functions are expressed in power form, i.e., each term, t<sub>i</sub>, has the form

$$t_i = c_i \prod_j x_j^{a_{ij}}$$
.

#### Problems Solved and Measures of Comparison

The geometric programs solved come from two sources: 8 problems given by Donbo in [2] and the 24 problems of Rijckaert and Martens in [6]. Problem sizes are given in Table 1 below. The problems are good examples of small, dense, highly nonlinear NLP's. The problems with some negative terms are generalized geometric programs with signomial constraints.

TABLE 1
Problem Size

Problem	No. of variables	No. of constraints	No. of positive terms	No. of negative terms	No. of binding constraints at optimality
D1	12	. 3	31	<b>o</b> 8	3 2
D2 D3	5	14	15 31		2
D4A,B	7 8 8 8	14 1 <sub>4</sub>	14	13 2	5 4
D4R, B D4C	8		16	0	<del>4</del> 5
D5	8	5 6	14	5	5 6
D6	13	13	27	5 <b>1</b> 2	11
D7	16	<b>1</b> 9	40	21	± ±
D8A,B		4	18	0	A: 2, B: 3, C: 4
Rl	4	2	6	0	2
<b>R</b> 2	3 4	1	9 12	0	1
R3		1	12	0	1 3 3 7 6
$\mathbb{R}^{4}$	11	3 3 7	30	0	3
R5	4	3	8	0	3
<b>R</b> 6	8 8	7	12	0	7
R7	Ö	7	12 48	0	
R8	(	7		0	2
R9	2 <b>2</b>	1	7 <del>1</del> 74	1 2	1 1
R10 R11	7 2 3 4	7	6	1	2
R12	8	2 4	13	2	4
R13	8	6	14	5	6
R14	10	6	13	5 2 3 3 5 4	6
R15	10	7	12	3	7
R16	10	7	13	3	7
R17	11	9	14	5	9
$\mathtt{Rl}8$	13	9	18		9
R19	8	5	26	2	9 5 <b>7</b>
R21	10	7	16	7	
<b>R</b> 22	9	10	36	2 <b>1</b>	7
R24	10	10	23	13	8

These may have local optima which are not global (such a point was encountered in at least one problem).

#### Measures of Comparison

In comparing GRG with the code used by Dembo in [2] (one of the better special purpose GP codes) two measures were available -- the final objective value obtained and the "standard time" required to achieve that value. Standard time is the execution time for the problem divided by the time to execute a timing program written by Colville [1]. This program inverts a 40 by 40 matrix 10 times. Use of standard time is supposed to compensate for the effects of different computing environments, e.g., machines, compilers, etc. To investigate this we solved 4 problems on the IBM 370/168 at Stanford University using three different FORTRAN compilers: the FORTRAN H compiler (OPT=2), the WATFIV compiler with the CHECK option and the WATFIV compiler with the NOCHECK option. The results appear in Table 2, which gives the times required by GRJ to solve four problems (with minimal printed output) divided by the time required to run the timing program. There is great variation in standard times between the three compliers, with widest variation (by factors of from 3 to 10) between WATFIV (CHECK) and the FORTRAN H compilers. Evidently this naive way of compensating for computing environment is inadequate. To compare with the other published results, we chose the WATFIV NOCHECK compiler, partly for convenience, partly because it gave the median times. In all GRG runs there was no printing of intermediate results, but input data and final results were printed.

TABLE 2
Standard Execution Times on Three FORTRAN Compilers

Problem	WATFIV (CHECK)	WATFIV (NOCHECK)	IBM FORTRAN H (OPT=2)
D <sub>7</sub> +C	0.026	0.052	0.109
D5	0.025	0.049	0.069
R2	0.005	0.012	0.038
R9	0.003	0.007	0.033
Colville Timing Program			
(IBM 370/168 c.p.u. seconds)	41.80	16.83	3.91

problems with run times less than 1 second, even this printing may consume a large fraction of total time.

Comparison with the Rijckaert and Martens results is difficult, since their starting points were chosen randomly, and were not published. We chose our starting values so that odd-subscripted variables were one-half their optimal value, and even-subscripted variables were three-halves their optimal value. The resulting points are shown in Appendix A.

### Computational Results

Table 3 shows the performance of GRG on the Dembo problems on our first attempt. Problem IA was too badly scaled to attempt solution, and the code failed on Problems 3, 6 and 7. In Problems 3 and 4, GRG terminated prematurely when no decrease in the objective was achieved while attempting to move in the direction of steepest descent, while in Problem 7 the program terminated short of feasibility at a local optimum of the Phase I objective.

Improved results were obtained by using an alternative pivoting strategy in computing the basis inverse. This strategy allowed pivoting on matrix elements smaller than allowed by the previous strategy if the alternative was entering a variable at a bound into the basis. This avoided degenerate bases in some cases, and allowed solution of problem 3 and improved performance on number 5 (see Table 4).

TABLE 3

Computational Results for Dembo GP Problems, Using Specified Constraint Tolerances

** Reason for	Term.		F.C.	K. 7.	ALPH=0	K.T.	E.	F.C.	۲. د.	ALPH=0		F.C.	F.C.	ы. С.
Newton*	AVB.	<b>7</b> h	.34	1.14	2.25	1.21	1.35	1.94	1,88	2.74		3,43	2.82 82	†0°†
Equiv. FCN Calls	(ne)	ed for GRG	369	24	<b>568</b>	285	560	304	302	577		1902	1249	<b>30</b> 09
Grad Calls	(ng)	Badly Scaled	15	9	15	18	<b>1</b> 6	17	16	21	e point	72	53	105
FCN Calls	(Ju)		189	17	163	141	132	168	174	304	nd feasible	1398	878	2274
Our	opt.		3.169247	10122.44	1453.23	3.951153	3,951165	3.95209	7049.54	261,16	Could not find	1809.763	911,8801	543.6681
Dembo	., do	4.890519	3,168213	10127,13	1227.18	3.951698	3.956197	3,95207	7049.32	97.5910	174.7888	1809.762	911.8796	543.6664
Dembo Std.	1 TIME	.2747	.2711	,0024	.0829	.2806	.1324	.0213	.1255	.3275	.2403	4560.	.0955	.0792
Std.	777		•055	.001	Įz4	.038	•024	.052	640.	Ĩ±,	ᅜ	.282	767	. 443
WATEIV Time		•	0.94	0.17	Es4	0.65	0.58	0.89	0.84	ᄄ	Œ	4.75	3.28	7.€
Prob.		<b>4</b>	9	2	3	<b>₽</b> ħ	<b>#</b>	<b>ş</b>	2	9	7	₩	<b>e</b>	ပ္တ

F = Failure

\*\* F.C. = Fractional charge in objective less than 10 tor 3 consecutive iterations

K.T. = Kuhn-Tucker point found to within 10-4

ALPH=0 = Premature termination--no function decrease in direction of steepest descent.

 $^{\dagger}$  Average number of Newton iterations per attempt to solve for basic variables.

 $\mathbf{1}_{\mathbf{f}}^{\dagger} \equiv \mathbf{Number}$  of function calls

where N = number of variables  $n_g = Number of gradient calls$  $<math>n_e = Equivalent function calls = n_e$ 

TABLE 4

Computational Results for Dembo GP Problems, Using Smaller Alternate Pivot

٠ ن	F.C.
2.10	2.28
375	277
21	14
228	165
1227.19	7049.6
1227,13	26,6407
6280.	.1255
750.	
0.96	
24	ın
	.057 .0829 1227.13 1227.19 228 21 375 2.10

Table 5 shows the effects of another modification to GRG.

The code uses the BFS variable metric method to minimize the reduced objective. The original strategy was to update the approximation, H, to the inverse hessian used by this method only when the line search terminated in an unconstrained optimum. Otherwise it was reset to the identity, and the search direction became the negative reduced gradient. The new strategy used the BFS update at each iteration, except those at which a basis change occurred. In the 5 problems of Table 5, this new strategy was better in all problems but one, significantly better in 3 problems.

Some Dembo problems (whose feasibility tolerance specified was tighter than  $10^{-4}$ ) were re-run using the default feasibility tolerance  $(10^{-4})$  of the GRG code. As shown in Table 6, solutions wer obtained faster than with the specified tolerances (Table 3). This prompted the use of a coarse tolerance to obtain an initial solution, followed by a refinement using the specified tolerances. As shown in Table 7, this strategy yielded a significant decrease in computational effort for Problems 8A, 8B and 8C.

The performance of GRG on the Rijckaert-Martens problems is shown in Table 8. The column "Reported S.T." contains the best standard time reported by Rijckaert and Martens [6] in a comparison of eleven special purpose codes for geometric programming and one general purpose code. GRG was generally slower than the best code and missed the true optimum by one to two percent in Problems 8, 13 and 15. Otherwise, GRG solved all these problems satisfactorily.

TABLE 5

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Computational Results for Selected GP Problems, Updating H-Matrix Whenever Possible

H-Matrix Updated

	pris.	H-Matrix Reset				H-Matrix Updated	dated	
Prob.	WATFIV Time	Our Opt.	Equiv. FCN Calls	Newton Avg.	WATFIV Time	Our Opt.	Equiv. FCN Calls	Newton Avg.
D8A D8B D8C	8.0.0 9.0.0 9.0.0 9.0.0	1809.428 911.536 543.5831	1526 810 1120	2.11 1.98 2.13	2.57 2.61 2.87	1309.007 911.6840 543.5853	973 973 1051	1.83 2.34 2.42
R1.4	6,11	1.1436	2939	3.15	2.65	1.1436	1217	2.55
R17	4.03	9011.	1445	1.99	2.70	.14228	1038	1.35

The Dembo problems above had a constraint tolerance of  $10^{**-\mbox{$4$}}$ .

TABLE 6

Computational Results for Dembo GP Problems, Using Constraint Tolerance of 10\*\*\_4

TOL=10\*\*\_4

	Newton Avg.	ብደ · O	000	7 2 0	t '.	, 0 t 0	70.1	,
ce	Equiv. FCN Calls	692	, ,	1 ( C (	2 6	12/10	3009	
Dembo Tolerance	Our Opt.	3.169247	1453.23	261.16	1809.763	911,8801	543.6681	
	WATFIV Time	16.0	Fε4	ᄕ	4.75		7.46	
	Tol.	10**-6	10**-5	10**-6	10**-6	70**-01	10**-6	
	Newton Avg.	6,1,0	1.64	1.53	2.11	1.98	2.13	
	Equiv. FCN Calls	230	219	501	1526	310	1120	
10L=10**44	Our Opt.	3.176152	1452.74	249.18	1809.428	911.5566	543.5831	
	WATFIV Time	0.61	Ħ	Ēų	3.36		3.08	
	Prob.	ro El	~	9	S.A.	8 <b>.</b>	<b>%</b>	

TABLE 7

The second secon

Computational Results for Dembo Problem No. 8,

ising loanse initial Constraint Folerance and First Foleranse of  $10^{-6}$ 

INTILL TOLETO\*\*\*4 INTEGEL TOL-10+-(

Frob.	EGW Calls	Grai Calls	Bquiv. Fon c.	Newton Avg.	FCN Calls	Gravi Calls	Equiv. Fon c.	Nevton Avg.	
85 848	r ∋6	0) 0)	1233	3.18	Ö	25	1630	1.74	
SB B	700	ές	5 <b>1</b> 77	<b>₹</b>	÷3		1053	υ () ()	
Çî j	1360	7: [**	1927	7.00.1	# <u>`</u>		1011	- F N. • UU	
		-							
Total	5 08 5 08 5 08	<del>,</del> <del>,</del> ,		Š.	J. C. S. C.	, H	31%	• • •	
	(C)	seconds	Total exemption Time		Print (erel )		Seconds		

The above runs include all improvements described.

TABLE 8

Computational Results for Rijckaert and Martens GF Problems

Notes	*		* *	I oo i da s
Reason for Term.	MERME EN	តុងគេ មុខកុកុង	AH AH HA HO HO DE	timographi os
Newton Avg.	1.52 1.39 0.0 1.40 0.16 1.26	1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00	2.53 1.99 ble point 1.94 1.04 2.05	unrecolued
Equiv. FCN C. (n <sub>e</sub> )	536 292 172 172 140 367	400 161 161 419 577 152	9 492 16 1445 17 527 17 527 13 590 17 484 16 320	2
$\frac{\texttt{Grad}}{(\mathbf{n_g})}$	25 25 25 20 20 20 20 20 20 20 20 20 20 20 20 20	21 13 13 13 13 18 18	אסטא טא	Prohlem 20 had
FCN Calls (nf)		253 229 124 109 219 272	302 939 Could 311 260 241	
Our Opt.	.01210. 6299.7 126306 3.1442 623277 29.2282	181.370 11.9002 -83.26 -5.7398 -6.0483 7082.93 1.1436 0.20566	.1966 .1406 .17485.9 -375.96	Was not rering
Their Opt.	.01208 6300 126344 3.1681 623015 29.5985	178.478 11.91 -63.21 -5.7398 -6.0482 7049.24 1.1436	.1966 .1406 .181818 17486. -1237.55	Tembo # C# Odmed
Their S.T.	.000. .000. .000. .000. .000. .000.		.019 .082 .054 .067 .094	ag dags
Std. Time	050. 900. 900. 410. 080.	.010 .010 .010 .052 .055		
WATFIV Time	0.52 0.05 41.0 0.04 0.04 0.04 0.05 1.36	0.93 0.93 0.85 0.86 0.11 0.12 0.13	1.16 .069 4.03 .239 1.51 .089 1.62 .096 1.68 .100 1.65 .062	50 me
Frob	Haran vo	ឆ្ ខ្លួន <b>ដូង</b> សូងូសូ	114 117 118 119 119 119	Drohlem

Problem 23 was the same as Dembo #2 so it was not rerun; Problem 20 had an unresolved typographical error. \*The feasibility tolerance used was  $10^{-14}$  in contrast to the stricter tolerance of  $10^{-5}$  used by Pijckaert and Martens. This difference would tend to bias results in favor of 3RG.

"Tolerance controlling termination had to be tightened by a power of 10.

Note that GMG is competitive or superior in its quandard time on the larger problems, 19 thru 14. Fince all times except two are on the order of 1 second, the printing of some output by 483 (which may consume a large fraction of run time in these cases and the previously mentioned difficulties with using standard times, haply that these comparisons must be taken with a large grain of salt.

An enhancement of the GRI code, described in [3], ares quadratic extrapolation to compute initial estimates of basic variables prior to solution of the nonlinear constraint equations in contrast to tangent vector extrapolation [4] used in the runs described above. Some of the Dembo and Rijckaert-Martens problems were used in tests to compare the two extrapolation schemes. The results, displayed in Tables 9 and 10, (which exhibit minor discrepancies with the results in Tables 3-5 owing to minor differences in tolerances and strategies used) show the superiority of quadratic extrapolation for these problems.

#### Conclusions

Conclusions to be drawn from these experiments are:

- 1. "Standard time," as defined by Colville in [1], is an inadequate means of compensating for different computing environments when attempting to compare optimization algorithms. Improved procedures are needed.
- well with special purpose geometric programming codes in solving geometric programs.

TABLE 9

Performance of GRG Using Tangent Vector Extrapolation

est blem 5.	Test Function Gr Problem Calls No. $(n_f)$	Gradient Calls (n)	Equiv. Function Calls (n <sub>e</sub> )	Newton Calls (NC)	Newton Failures (NF)	Newton Iterations (NI)	Newton Average NI/(NC-NF)	Execution Time (Sec.)	Standard
	17	9	24	~	0	8	1.14	0.18	0.0107
	141	18	285	99	<b>,</b> -1	68	1.24	92.0	0.0452
	165	17	277	23	8	114	2.43	0.75	9440.0
	1398	72	1902	308	8	1057	4.26	5.17	0.3072
	231	19	383	75	†7	139	1.96	1.48	6.0879
	253	21	7,00	59	9	186	3.51	3.15	0.1872
	219	25	419	93	ঝ	117	1.31	1.01	0.0600
	029	45	1120	182	77	465	5.66	3.21	0.1307
	272	18	452	. 87	7	185	2.50	1.21	0.0719
	302	19	764	83	5	210	2.69	1.27	0.755
8.1	Total 3668	257	5777	1.6	76	2549	2.84	18.19	1.0808

TABLE 10

Performance of GRG Using Quadratic Extrapolation

Standard Time	0.0107	0.0446	0.044C	5.24%	0.0868	o. o529	0.0529	C. 1467	0.0707	0.0766	0,8354
Execution Time (Sec.)	0.18	0.75	0.74	4.20	1.46	6.83	0.89	2.47	1.19	1.29	14.06
Newton Average NI/(NC-NF)	1.14	0.51	5.00	3.16	1.64	2.54	ું	2.29	5.14	1.89	2.20
Newton Iterations (NI)	ω	51	き	743	121	132	42	291	163	157	5637
Newton Failures (NF)	0	-	<b>M</b>	54	2	9	-1		₹	CU	77
Newton Calls (NC)	2	56	50	278	75	58	82	138	81	8	41%
Equiv. Function Calls (n <sub>e</sub> )	1.4	268	257	1488	598	231	346	822	433	151	3500
Test Function Gradient Problem Calls Calls No. $\langle n_{\mathbf{f}} \rangle$	9	87	17	62	15	27	22	37	18	50	235
Function Calls (n <sub>f</sub> )	17	ή <b>2</b> Ι	145	1054	217	88	170	452	253	251	2881
Test Problem No.	8	DAA	55	D8A	R6	38	RIZ	R14	R15	R16	TOTAL

22.7

22.7

21.5

27.8

25.7

2.8

4.6%

ب عأدة

21.5

% Reduction in Total from Tangent Vertor Extrapolation

- 5. Certain modifications in solution strategy can strongly affect the performance of GRG. Among these are: when the approximate hessian is reset, the logic used in basis inversion to decide when a variable at bound is to enter the basis, and the order of extrapolation (linear or quadratic) used to obtain initial estimates of the basic variables.
- 4. Certain parameter settings strongly affect GRG performance: in particular, the tolerance used to determine which constraints are binding, and the tolerance used to terminate the algorithm.

In closing, we note some things left undone but worth doing. GRG could easily be made more convenient and efficient on geometric programs by coding a special subroutine to compute first partial derivatives. This would use the fact, that if the ith term in the program is

$$t_{i} = c_{i} \prod_{j=1}^{n} x_{j}^{a_{ij}}$$

then

$$\frac{\partial \mathbf{t_i}}{\partial \mathbf{x_k}} = \frac{\mathbf{a_{ik}t_i}}{\mathbf{x_k}}$$

Hence, if the terms are stored when computing the constraint and objective values, their partial derivatives are available with little additional effort. This would reduce the time required to compute the gradient of a function from the time required in these runs  $(nt_f)$ , where  $t_f$  is the time required to evaluate the function and n is the number of variables) to little more than  $t_f$ . Special input subroutines could

be coded to enable the user to specify the problem by inputting only

(a) the constants  $c_i$ , (b) the exponent matrix  $a_{i,j}$  and (c) which terms appear in which problem functions. Currently, all problem functions must be coded directly. These enhancements would transform Gkd into a "special purpose" geometric programming code.

Some additional experiments appear useful. Geometric programs can be transformed into exponential form by the change of variables

$$x_j = e^{y_j}$$

which transforms the ith term into

$$t_{i} = c_{i} \exp(\sum_{j} a_{ij} y_{j})$$

Evaluation of  $t_i$  then requires only one transcendental computation rather than one for each fractional  $a_{i,j}$ . In addition,  $y_j$  is a free variable (if  $x_j$  has no upper bound), and the problem functions become convex if all  $c_i$  are positive. Some problems should be solved using both forms, to see Which yields smallest solution times. In addition, tests of GRG and some good geometric programming codes should be run on the same computer, in order to remove the factor of standard times from obscuring the comparisons.

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# APPENDIX A

# Starting Values of Variables Used for the Rijckaert-Martens Problems in GRG Runs

Problem No.	
1	41.0, 140,0, 4.1, 2.1
2	54.0, 126.0, 102.0
3	375.0, 0.17, 0.73, 5.1
),	1.25, 3.75, 3.8, 1.8, 3.9, 1.95, 2.14, 4.2, 0.85, 3.0, 3.3
5	21.5, 67.0, 33.0, 1.6
6	0.5, 0.3, 0.56, 1.1, 0.5, 1.05, 0.56, 1.5
7	0.5, 0.3, 0.56, 1.1, 0.5, 1.05, 0.56, 1.5
8	0.67, 1.5, 0.44, 1.38, 1.57, 0.6, 0.77
9	0.41, 660.0
10	44.1, 11.0, 0.65
11	4.66, 1.23, 0.28, 2.82
12	3.23, 1.32, 0.51, 8.99, 1.11, 0.9, 0.2, 8.3
13	290.0, 2040.0, 2550,0, 273.0, 148.0, 327.0, 143.0, 594.0
14	1.05, 13.15, 3.95, 0.69, 0.18, 0.69, 3.22, 2.46, 0.60, 0.65
15	0.36, 1.08, 0.36, 0.39, 0.09, 0.15, 0.1, 0.21, 0.05, 0.45
16	0.36, 1.00, 0.36, 0.39, 0.09, 0.18, 0.1, 0.21, 0.05, 0.45
17	3.5, 11.4, 3.7, 0.62, 0.4, 1.5, 0.15, 0.55, 0.18, 3.0, 0.23
18	0.2, 0.21, 0.1, 0.96, 0.3, 0.5, 0.003, 0.04, 0.26, 2.8, 1.2, 0.24, 0.17
19	2600.0.9.9, 80000.0, 1000.0, 44000.0, 874.0, 6.06, 45.0
51	900.0, 9000.0, 45.0, 4500.0, 1000.0, 2.0, 92.0, 0.0, 1.5, 150.0
22	5.9, 0.5, 0.68, 6.1, 60.0, 0.2, 50.0, 0.36, 0.36
24	0.4, 1.0, 0.9, 0.05, 0.38, 0.11, 1000.0, 37.0, 750.0, 0.2

Unclassified
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20. Abstract. SOL 76-1
This paper describes the performance of a general purpose GRG code for nonlinear programming in solving geometric programs. The main conclusions drawn from the experiments reported are:
(A) GRG competes well with special purpose geometric programming codes in solving geometric programs and,  "Standard Time," as defined by Colville, is an inadequate means of compensating for different computing environments while comparing optimization algorithms.